Swap motion–directed twinning of nanocrystals

Qiubo Zhang†, Zhigang Song†, Yu Wang†, Yifan Nie†, Jiawei Wan†, Karen C. Bustillo‡, Peter Ercius‡, Linwang Wang†, Litao Sun§, Haimei Zheng†,*

Twining frequently occurs in nanocrystals during various thermal, chemical, or mechanical processes. However, the nucleation and propagation mechanisms of twinning in nanocrystals remain poorly understood. Through in situ atomic resolution transmission electron microscopy observation at millisecond temporal resolution, we show the twinning in Pb individual nanocrystals via a double-layer swap motion where two adjacent atomic layers shift relative to one another. The swap motion results in twin nucleation, and it also serves as a basic unit of movement for twin propagation. Our calculations reveal that the swap motion is a phonon eigenmode of the face-centered cubic crystal structure of Pb, and it is enhanced by the quantum size effect of nanocrystals.

INTRODUCTION

Twinning is one of the most common structural transformations of nanocrystals responding to external stimuli, including mechanical loading (1), electron beam or ion irradiation (2, 3), laser shocking (4), and heating (5). Nanocrystals with twin structures may yield superior properties, such as excellent mechanical strength (6), improved thermal stability (7), high electrical conductivity (8), remarkable light emission (9), and enhanced catalytic activity (10). Understanding the twinning mechanisms in nanocrystals enables the structural engineering of nanomaterials with desired properties.

Conventional wisdom holds that twinning proceeds via layer-by-layer movement of partial dislocations on adjacent atomic planes (11). Deformation twinning under external mechanical loading involves unconventional mechanisms, described as random activation of partial dislocations (12), simultaneous activation of partial dislocations (13), or a shuffle mechanism (14). Transformation twinning induced by the external stimulus other than mechanical loading is less well understood. It is assumed that the transformation twinning of nanocrystals proceeds through the traditional deformation twinning mechanism (11); however, this claim lacks direct evidence. Transformation twinning requires external energy to overcome the energy barrier (2–5). The injection of external energy (15, 16), such as during thermal annealing and electron or ion irradiation, provides opportunities for the twin formation in nanocrystals. This indicates that the twinning of nanocrystals may exhibit nonconventional pathways controlled by kinetics. However, because the speed of partial dislocation/slip is considered to occur on time scales as fast as the speed of sound (17), simultaneously realizing twinning excitation and atomic imaging is still a technical challenge.

In this work, with face-centered cubic lead (Pb) nanoparticles as a model system, we investigate the transformation twinning in individual nanocrystals using transmission electron microscopy (TEM) with atomic spatial resolution and millisecond temporal resolution. Compared with other materials, Pb nanocrystals have a low melting point and are not easily oxidized, so it is ideal for driving structural transformations through controlled electron beam irradiation. To obtain a high temporal resolution, we used advanced aberration-corrected TEMs: one equipped with a Gatan K2 IS camera at 400 frames per second (fps) and the other equipped with a high-speed Thermo Fisher Scientific Ceta camera at 40 fps (18).

RESULTS

As shown in Fig. 1, we can observe the structure of a Pb nanocrystal as it transforms between a single crystal and a twinned crystal. The Pb nanocrystals are grown on lead titanate substrates by electron beam irradiation (figs. S1 to S4 and movie S1). They are typically in a truncated octahedral shape, and a two-dimensional (2D) projection along the [01T] direction is composed of four [111] and two [200] planes (Fig. 1A). On the basis of our examination of 36 nanocrystals, we determined that there are an average of 18 and 20 atomic layers in the (111) and (200) directions (Fig. 1B), respectively. During in situ imaging, the electron beam drives the structural transformation of Pb nanocrystals. Structural oscillations between the single and twinned crystals can be modulated by electron beam dose and temperature (fig. S5). We did control experiments to elucidate the origin of transformation twining in Pb nanocrystals. The results show that the formation of transformation twin is dependent on electron beam current density (fig. S5). In addition, under the same electron beam current density but at cryogenic temperature, no obvious structural fluctuations are observed (fig. S6 and movie S2). These suggest that the transformation twinning arises from the enhanced thermal vibration induced by the high-energy electron beam. As shown in the representative image sequence (Fig. 1C and movie S3), a single crystal undergoing twin nucleation forms a three-layer twin embryo (0 to 0.1 s), and it propagates to become a single twin (0.1 to 0.15 s). Subsequently, the structure fluctuates between multiple parallel twins and single twins (0.15 to 0.5 s) and finally returns to a single crystal (0.5 to 0.75 s). The corresponding fast Fourier transform (FFT) images confirm the conversion between the single and twinned crystals (Fig. 1D). The trajectory of recurrent structural transformations between the single crystal and the twinned crystal can further confirm this phenomenon (Fig. 1E). Under the electron beam illumination, the Pb particle is always in a high-energy state. Nanocrystals dissipate extra energy by phonon...
vibration (19, 20), inducing the fluctuations between single and twinned crystals, accompanied by the nucleation and propagation of twins. The ratio of retention time of single crystal to twinned crystal is about 3 to 2 (Fig. 1F). We consider that the single crystal is more stable than the twinned crystal in terms of energetics (21). Thus, the single-crystal structure tends to last longer.

Figure 2 shows the atomic pathway of two-layer swap motion, which dominates the nucleation of a three-layer twin embryo (movie S4). Because of the fast speed of partial dislocation propagation and slip of two atomic layers (17), the nucleation of a three-layer twin embryo usually completes within one frame of our movies. To observe the atomic details of the swap motion, we use grain boundaries as obstacles to dislocation motion (22). Here, we focus on the highlighted red square area in Fig. 2A to study the formation of one twin embryo. We use computer vision to recognize atom positions at each frame and build ball models based on the computer-identified sites (figs. S7 to S9). They are then stacked together to visualize the atom dynamics (Fig. 2B). We found that the atomic pathway of twin nucleation is markedly different from that of deformation twinning (fig. S10) (11–14, 23, 24). Comparing the atom positions at 0 and 0.3 s, we show that part of the atoms in the second layer slip to the left, pinning the crystal, and a plug dislocation (dislocation pileup) forms at the movement front. The plug dislocation moves left over time. When it approaches the left end, almost all atoms in the second layer are right above the atoms in the third layer, repelling them to the right. At the final step, the second and third atomic layers move slightly to the right, adjusting themselves to form a twin embryo. At 4.1 s, some atoms fill the high-energy atom steps. These atoms are presumed to diffuse through the surface. Figure 2C shows the shift distance of each layer over time, and the
frames from either right-tilt (P1 to P3) or square (P4 to P13). The resistance to swap motion from a local defect. Once overcoming the (from left to right) fluctuates between 35° and 10°, reflecting the critical for the twinning process. The change in tilt angle over time is shown in Fig. 2E. Note that the tilt angle of the third parallelogram atoms only shifted left by 0.7 Å from 0 to 0.3 s, it already changes the phase state of first- and second-layer atoms from right tilt (0°). In summary, the second and third layers move about 1 Å in opposite directions, as if they had swapped positions, so we name it “swap motion.”

From another perspective, the twinning process resembles the evolution of a phase transition. As shown in Fig. 2B, the transition state from 0.3 to 3.0 s exhibits a considerable difference in local phase states. We evaluate the local phase by analyzing the shape of the parallelograms formed by four adjacent atoms. For instance, Fig. 2D shows the quantitative color map of the tilt angles of all parallelograms at 0.3 s. Tilt angles of parallelograms are calculated from two vertical edges, and the color map shows the transition from tilting left (orange), upright (gray), to tilting right (blue). (E) The evolution trajectories of the tilt angles of each parallelogram between the second and third layers. Thirteen parallelograms are labeled as P1 to P13 from left to right.

small boxes show the ideal positions after twinning. Although, at 3.4 s, the first and fourth layers have slightly shifted because of internal strain, they return to the original position after structural self-adjustment at 4.1 s. From 0 to 3 s, the second layer moves to the left, and the third layer does not change. Only after the second layer crosses over the top of the third layer that the third layer starts to slide to the right (3 to 4.1 s). In summary, the second and third layers move about 1 Å in opposite directions, as if they had swapped positions, so we name it “swap motion.”

The statistical results show that most twinning nucleation proceeds through this swap motion (fig. S11).

The swap motion not only dominates the twinning nucleation but also serves as a basic unit of movement for the propagation of twinning. Some atom layers are blurred, indicating that atoms moved during single-frame acquisition, as shown by TEM simulation (figs. S12 to S14). Figure 3 suggests that a single crystal can form twins of any layers through swap motion and partial dislocation slipping units. In Fig. 3, A and B are two basic movement units. For the swap motion (Fig. 3A), the two mobile layers slip 1/6 [1 1 2] along opposite directions. For the partial dislocation motion (Fig. 3B), all layers above the slip plane slip with a Burgers vector of 1/6 [1 1 2]. For face-centered cubic crystals, the unit cell has three atomic layers in the [1 1 1] direction. We can divide nanotwins into three categories based on the remainder of the number of layers divided by 3. If the remainder is 2, then the twinning can be completed by multiple swap motions (at least one), one of which occurs at the edge (Fig. 3C and figs. S15 and S16). As more swap motions happen in the middle of the nanoparticle, the 2-layer twin can transform into twins with 2 + 3X layers (X is an integer greater than 0). If the remainder is 0, all swap motions to achieve twinning occur in the middle (Fig. 3D and figs. S17 and S18). As more swap motions happen, the 3-layer twin can become twins with 3 + 3X layers (fig. S18). If the remainder is 1, for example, it forms a four-layer twin, except for one step of swap motion, then a partial dislocation slipping motion is also needed (Fig. 3E and fig. S19). With more swap motions occurring in the middle, the 4-layer twin can turn into twins with 4 + 3X layers. Table S1 demonstrates a comprehensive road map for twin formation.

### Table S1: Twinning Process Summary

<table>
<thead>
<tr>
<th>Layer</th>
<th>Number of Layers</th>
<th>Twinning Pathway</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st</td>
<td>1</td>
<td>Single Swap</td>
</tr>
<tr>
<td>2nd</td>
<td>2</td>
<td>Single Swap</td>
</tr>
<tr>
<td>3rd</td>
<td>3</td>
<td>Single Swap</td>
</tr>
<tr>
<td>4th</td>
<td>4</td>
<td>Single Swap</td>
</tr>
</tbody>
</table>

Zhang et al., Sci. Adv. 8, eabp9970 (2022)  7 October 2022
Here, we take the formation of a 12-layer twin as an example to show the propagation of twins (Fig. 3F and movie S5). First, a single crystal undergoes two swap motions simultaneously, forming a six-layer twin. Then, it takes another swap motion and turns into a fourfold parallel twin. In the end, the two atom layers between the 3-layer twin and the 6-layer twin swap positions result in a 12-layer twin. Note that we found that the swap motions can occur simultaneously or subsequently within a nanocrystal. In addition, the swap motion can be initiated in multiple locations within a nanocrystal to form spaced twin domains (as shown in Fig. 3F). By swap motion, the structure can transform between twins with different numbers of layers.

**DISCUSSION**

To further understand the dynamics, we performed phonon calculations based on density functional theory (DFT). Figure 4A shows the calculated phonon band structure of a Pb nanocrystal. Each phonon mode propagates in a certain momentum indicated by the horizontal axis and oscillates at a specific frequency (namely, energy). The phonon band structure shows a valley at point T, which implies that the phonon mode at point T is soft. The wavelength of the phonons at point T is the shortest, and it is about three atomic layers (~1 nm). Amazingly, one of the eigenmodes at the position marked by a green star in Fig. 4A is a swap mode (Fig. 4B), which indicates that the swap mode is intrinsic. Because of the quantum size effect, the long-wavelength phonons are forbidden. Only phonons whose wavelength is smaller than the diameter of nanocrystals are allowed. Thus, the size effect of nanocrystals enhances the swap modes. The diameters of our Pb nanocrystals are around 10 nm. According to previous work (2, 15), electron beam irradiation can influence the sample by increasing the local thermal vibration. At a finite temperature, the density of short-wavelength low-energy phonons is very high. The probability is described by

\[ P \propto \frac{L}{\lambda^2 e^{\omega/k_B T} - 1} \]
Synthesis of \( \text{PbTiO}_3 \) nanorods

We synthesized the PX-phase lead titanate (\( \text{PbTiO}_3 \)) nanorods by a hydrothermal method (25). Typically, 4 mmol Ti(OC\(_4\)H\(_9\))\(_4\) was first dissolved in a mixed solution of 8 ml of ethanol and 8 ml of deionized H\(_2\)O. Subsequently, 20 mmol KOH, 5.2 mmol Pb(CH\(_3\)COOH)\(_2\)•3H\(_2\)O, and 0.05 g of polyvinyl alcohol were added to the solution and mixed homogeneously under vigorous stirring. Then, we adjusted the volume of the final feedstock to 40 ml with deionized H\(_2\)O. The ratio of Pb/Ti in the starting materials was kept to 1.3 to ensure a complete reaction of TiO\(_2\)•3H\(_2\)O gel. Then, the solution was transferred to a Teflon-lined stainless steel autoclave, and the autoclave was sealed and heated at 200°C for 3.5 hours, after which it was allowed to cool to room temperature naturally. The products were isolated by centrifugation at 6000 rpm for 10 min and washed with deionized H\(_2\)O until a neutral pH was achieved and then washed in 10 weight % CH\(_3\)COOH aqueous solutions to remove the remnant PbO. The final pure PX-phase sample was obtained by another cycle of washing with deionized water and dried at 60°C in air. The structural characterization of as-synthesized \( \text{PbTiO}_3 \) nanorods (fig. S1) shows a well-defined single-crystal structure.

**MATERIALS AND METHODS**

**Experimental design: Why choose electron beam–induced twinning of nanocrystals**

In these experiments, the electron beam provided the external stimuli to inject energy into the nanocrystal. Rather than heat the entire sample to induce the structural fluctuations between single-crystal and twin-crystal structures, electron beam excitation can reduce the complexity of the research system, and it is easy to control the electron beam intensity in situ. To study the twinning mechanisms of \( \text{Pb} \) nanocrystals at atomic resolution, the zone axis of the crystal must be along the [110] direction. To slow the dislocation motion central to the twinning process, we used the interface between the Pb particles and the PbTiO\(_3\) substrate to block the slip movement of dislocations. No ligands were attached to the surface of the particles prepared by the in situ method, which eliminated the influence of ligands on the twinning of nanocrystals. By slowing the process and using the 1.6- to 2.5-ms cameras, we were able to obtain the data resulting from our models.

**Electron microscopy characterization**

Most of the movies were acquired by the ThemIS (operated at 300 kV), a Thermo Fisher Scientific TEM equipped with an extreme field emission gun (X-FEG) gun, an image aberration corrector, and a high-speed FEI Ceta2 scintillator-coupled complementary metal-oxide semiconductor camera. The Ceta2 is capable of capturing 2048 × 2048 resolution images at ~40 fps. To increase the frame
rate, we also tried the electrostatic subframing system of ThemIS, which can achieve high temporal resolution as high as 1.6 ms.

Other movies were acquired by the transmission electron aberration-corrected microscope 1, a modified Thermo Fisher Scientific Titan TEM equipped with a high-brightness Schottky field-emission electron source (X-FEG), spherical- and chromatic-aberration corrector, and a Gatan K2 IS direct electron detector at the National Center for Electron Microscopy within the Molecular Foundry in Lawrence Berkeley National Laboratory. Using the direct electron detector, images of 1920 × 1792 (pixel size, 0.0203 nm) were captured every 2.5 ms. Energy-dispersive x-ray spectroscopy (EDS) data were acquired by the ThemIS equipped with a high-angle annular dark-field detector and four EDS detectors.

**Methods to differentiate twinning via conventional or swap motion paths**

For the two-layer twin formation (fig. S20), the top two layers first slip together by $\frac{1}{3} [112]$, and then, the first layer shifts $\frac{2}{3} [112]$ in the classical pathway. Thus, in the TEM image, either the top two layers or the first layer is blurred due to the fast movement. In addition, it is impossible that only the second layer is blurred. However, in the swap pathway, the two atomic layers can move successively or simultaneously, so it is possible that only the second layer is blurred.

For the three-layer twin formation (fig. S21), the top three layers first slip by $\frac{1}{3} [112]$, then the top two layers shift $\frac{2}{3} [112]$, and, lastly, the first layer shifts $\frac{1}{3} [112]$ in the classical pathway. Hence, atomic vacancy on the right side of the first layer will remain on the right side. However, in the swap pathway, the first layer does not move, and only the second atom layer and the third atom layer exchange positions. Therefore, the atomic vacancy in the first layer will transfer from the right end to the left end. Similar to the formation of two-layer twins, both the second and third layer blurring can only occur through the swap pathway.

In the same way, for the formation of four-layer twins (fig. S22), the blurring of the first, third, and fourth layers can only occur through the swap pathway. The atomic vacancy of the first layer that transferred from the right end to the left end further confirms the swap motion.

**Theoretical calculation**

We performed the calculation of phonon band structure and eigenmodes using the PWmat package based on a plane-wave basis set. The plane waves are cut off at 50 rydberg. SG15 pseudopotential and Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional are applied. The atomic positions are fully relaxed until the force on each atom is below 0.001 eV Å$^{-1}$ T$^{-1}$, and then, the force constant is calculated in the finite displacement method. A supercell of 3 × 3 × 3 is applied. The phonon bands are calculated by Phonopy.

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at https://science.org/doi/10.1126/sciadv.aba9970

**REFERENCES AND NOTES**


Acknowledgments

Funding: This work was supported by the U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences (BES), Materials Sciences and Engineering Division, under contract no. DE-AC02-05-CH11231 within the in situ TEM program (KC22ZH). Work at the Molecular Foundry of Lawrence Berkeley National Laboratory (LBNL) was supported by the U.S. Department of Energy under contract no. DE-AC02-05CH11231. Author contributions: Conceptualization: Q.Z. and H.Z. Methodology: Q.Z., Y.W., Z.S., Y.N., P.E., L.W., and L.S. Visualization: Q.Z., Y.W., Z.S., Y.N., and P.E. Funding acquisition: H.Z., L.W., and P.E. Project administration: H.Z. Supervision: H.Z. Writing—original draft: Q.Z., Y.W., and Z.S. Writing—review and editing: H.Z., L.S., K.C.B., P.E., and J.W. Competing interests: The authors declare that they have no competing interests. Data and materials availability: All data needed to evaluate the conclusions in the paper are present in the paper and/or the Supplementary Materials.
Swap motion–directed twinning of nanocrystals
Qiubo Zhang, Zhigang Song, Yu Wang, Yifan Nie, Jiawei Wan, Karen C. Bustillo, Peter Ercius, Linwang Wang, Litao Sun, and Haimei Zheng

DOI: 10.1126/sciadv.abp9970

View the article online
https://www.science.org/doi/10.1126/sciadv.abp9970
Permissions
https://www.science.org/help/reprints-and-permissions